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"LYAPUNOV (LIAPOUNOFF) AND POINCARÉ'S METHODS IN
THE THEORY OF NONLINEAR OSCILLATIONS"

I. G. Malkin

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